

# Behavioral Spillovers and Cognitive Load in Multiple Games: An Experimental Study\*

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## Abstract

We present evidence from laboratory experiments of behavioral spillovers and cognitive load that spread across strategic contexts. In the experiments, subjects play two distinct games simultaneously with different opponents. We find that the strategies chosen and the efficiency of outcomes in one game depends on the other game that the subject plays in predictable directions. Using outcome *entropy* to measure behavioral variation in a normal form game, we find that prevalent strategies in games with low outcome entropy are more likely to be used in the games with high outcome entropy, but not vice versa. Taken together, these findings suggest that people may not treat strategic situations in isolation, but may instead develop heuristics that they apply across games.

Keywords: multiple games, behavioral spillover, cognitive load, entropy, experiment  
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# 1 Introduction

In this paper, we describe laboratory experiments in which individuals simultaneously and repeatedly play two games with different opponents. We test whether an individual's play in one game is influenced by the other strategic interaction she faces. Multiple games can increase cognitive load preventing individuals from choosing efficient or even equilibrium behaviors. They can also induce behavioral spillovers in which individuals choose similar strategies in the two games. We find evidence of both psychological processes.

First, we find that although individuals are free to apply distinct strategies in each game, they instead develop and apply common behaviors across the two games. For example, when playing the prisoner's dilemma paired with a game of chicken, players alternate on the off-diagonals more often than they cooperate, as compared to when the prisoner's dilemma is played alone. Thus, behavior in one game appears to spill over into the second game.

The extent and direction of that spillover appear to depend on the complexity of the outcome dynamics. Yet, to the best of our knowledge, we could not find in the literature any measure of game complexity. We, therefore, propose that *entropy* of outcomes suffices as a measure of complexity. Entropy captures behavioral variation, which should be correlated with the cognitive load induced by the game. For example, a game with a dominant strategy, efficient equilibrium is not complex. In the control sessions, when subjects play a single game of this type, the play of this game produces the same outcome in almost every period, and therefore has low entropy. Thus, using entropy as a measure, this game is less cognitively taxing than a prisoners' dilemma game, which produces substantial behavioral variation.

In our experiments, we compare outcomes in single-game controls to outcomes in two-game ensembles, as well as outcomes between ensembles. Using entropy of outcomes measured in the single-game control sessions, we can then make *out-of-sample* forecast of game play in treatments with two-game ensembles. We find that, in these two-game ensembles, prevalent strategies in games with low entropy are more likely to be used in the games with high entropy, but not vice versa.<sup>1</sup> In other words, spillovers subjects apply strategies developed for easier games and apply them to more complex games.

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<sup>1</sup>Our results are distinct from but complement earlier research on sequential behavioral spillovers, which have been interpreted as a form of priming or framing (Tversky and Kahneman 1986).

The subjects' performance in the two-game ensembles supports both cognitive load and behavioral spillovers. By the former, we mean that individuals prove not up to the task of playing both games optimally. By the latter, we mean that strategies in one game bleed over into the other game. Cognitive load need not imply behavioral spillovers. A subject suffering from overload could opt to play a simple strategy unrelated to her strategy in the other game. Nor is cognitive load necessary for behavioral spillovers. For example, cooperation in the prisoners' dilemma could be enforced through either Tit for Tat or a grim trigger strategy. Either of these strategies could behaviorally align with an efficient strategy in some other game. Thus, the spillover would exist even though the subjects were not overloaded. That said, spillovers do imply a cognitive cost reduction. And, given the games that we consider in this paper, the spillovers that we identify all include loss of efficiency, which is consistent with cognitive load.

To test for behavioral spillovers we posit hypotheses that are distinct from those that would be created by cognitive load alone. As just mentioned, cognitive load would imply that behavior varies significantly from control sessions when multiple games are played simultaneously but that the form of that variation would be independent of the other game in the ensemble (provided that game demands equal cognitive attention). Yet, we find that behavior in one game depends significantly and predictably upon what other game is included in the two-game ensemble. This finding suggests that variance in actions cannot be attributed exclusively to cognitive load but instead indicates the presence of behavioral spillovers.

Our findings have an important implication for the study of games and for social science research more generally. If behavior in one game depends on other games an individual plays, then social scientists, whether doing experimental, theoretical, or empirical research, may need to consider the full ensemble of games that an individual faces (Samuelson 2001, Bednar and Page 2007). To date, almost all game theory research focuses on individual games, as do most experiments. That norm is changing. A recent flurry of multiple game experiments demonstrates the existence and magnitude of ensemble effects. Our theory of behavioral spillovers can explain some of the findings in these experiments (Section 2).

The interest in multiple game experiments can be attributed partly to their ability to generate deeper insights into both individual and collective behavior. For learning about individual behavior, these experiments provide a laboratory in which subjects find themselves in a more cognitively

taxing environment, one that resembles real world situations in which multiple stimuli simultaneously demand a person's attention. At the collective level, the findings from multiple game experiments may contribute to an institutional explanation for behavioral variations in the play of common games. Distinct sets of experiences or cases lead distinct communities to draw different analogies when constructing strategies (Gilboa and Schmeidler 1995). Institutional interventions that take into account the behavioral repertoire of the relevant individuals may be more likely to succeed. A better understanding of behavioral spillovers can contribute to the analyses and design of institutions.

We have organized the paper as follows. In Section 2, we summarize the relevant theoretical and experimental literature. Section 3 describes the specific games included in this study and our experimental design. Somewhat unusually, in Section 4 we first present the results from the control sessions, where participants play a single game, and then develop our multiple-game hypotheses in Section 5, which are based on theory as well as results from the control sessions. Section 6 reports our findings on the ensemble effects. In Section 7, we discuss what these findings might mean and comment on potential future directions.

## **2 Literature Review**

In this section, we review the theoretical and experimental literature on multiple games. Samuelson (2001) formally models behavioral spillovers and cognitive load when people play multiple games. He assumes that people pay a cognitive cost to analyze a strategic interaction. More sophisticated analyses require more cognitive load. In his model, individuals maintain a stock of analogies to organize their reasoning. In the analysis of three different bargaining games, the ultimatum game, the Rubinstein (1982) alternating offer bargaining game, and a tournament, he characterizes two equilibria, one in which the two bargaining games are played separately, and one in which they are played jointly. In the latter, players apply common analogies to disparate bargaining situations.

Samuelson's analysis is restricted to bargaining games. Bednar and Page (2007) examine behavioral spillovers and cognitive load effects in a broader class of six  $2 \times 2$  games. They prove conditions for the existence and efficiency of behavioral externalities, using computational agent based models (Miller and Page 2007). Their agent based models show that simple learning rules could

locate the proposed equilibria when played in isolation. When agents needed to solve multiple games simultaneously, the agents often created routines that they applied across strategic domains. The agent based model generates behavioral spillovers; agents employed identical strategies in distinct games. The model also shows evidence of cognitive load: some ensembles of games outstrip the capacity of the agents to play each game optimally. In those cases, they find especially strong ensemble effects. Given their focus on ensemble effects, Bednar and Page (2007) provide the main theoretical foundation for the current paper.

In comparison to the action-bundling results of Samuelson (2001) and Bednar and Page (2007), Jehiel (2005) uses a belief-bundling approach, where a player forms expectations about the behavior of the other players by pooling together several contingencies (analogy class) in which these other players must move, and forms an expectation about the average behavior in each analogy class. In his analogy-based expectation equilibrium, a player with coarser beliefs could still adopt different actions in different normal form games.

We now review the emerging multiple games experiments, and use our entropy measure to explain some of the findings in these experiments. Falk, Fischbacher and Gaechter (2010) investigate social interaction effects when two identical coordination or public goods games are played simultaneously with different opponents, and find no behavioral spillovers between the two games, which is consistent with our prediction that two identical games with the same entropy should not influence each other. In comparison, Savikhin and Sheremeta (2010) study simultaneous play of a public goods game (low entropy) and a competitive lottery contest (high entropy). They find that cooperation in the public goods game reduces overbidding in the lottery, while contributions to the public good are not affected by the simultaneous participation in the lottery. This result is consistent with our prediction that game influence flows from low entropy games to high entropy games. In a third study, using both a sequential and a simultaneous treatment, Cason, Savikhin and Sheremeta (2010) report cooperation spillovers from the median-effort game (low entropy) to the subsequent minimum-effort game (high entropy) when the games are played sequentially, but not simultaneously. Again, this result is consistent with our predictions based on entropy. Finally, Cason and Gangadharan (2010) investigate behavioral spillovers between a threshold public goods game and a competitive double auction market. They find that cooperation in public goods provision is less common when players simultaneously compete in the market.

There also exist sequential multiple games experiments. These studies identify significant framing (Tversky and Kahneman 1986) and learning transfer effects. Both of these phenomena are related to behavioral spillovers (Cooper and Kagel 2008, Haruvy and Stahl 2010). Consider the experiments that first auction off the right to play in a game. These experiments produce different outcomes in subsequent games. If we think of the auction as an initial game, we can interpret the resulting improved outcomes as resulting from some sort of behavioral spillover. For example, Van Huyck, Battalio and Beil (1993) demonstrate that without a pre-play auction, the median-effort coordination game played in isolation leads to inefficient equilibrium but that auctioning off the right to play before the coordination game leads to the payoff-dominant equilibrium. Crawford and Broseta (1998) explore the efficiency-enhancing effect of auctions theoretically using a model of stochastic, history-dependent learning dynamics, giving an analytic explanation for these results.<sup>2</sup> Lastly, Huck, Jehiel and Rutter (2010) study feedback spillovers in sequential multiple games and find empirical support for an analogy-based expectation equilibrium (Jehiel 2005). They use a different protocol from the multiple game experiments discussed above. In their experiment, a player plays one of two games in each round, and sometimes receives the aggregate distribution of the play of the opponents over the two games, a design feature aimed to compare the long-run behavior in the presence and absence of feedback spillovers. Grimm and Mengel (2010) use a similar protocol where a player plays one of several games each round, and find that their data can be rationalized by either action- or belief-bundling.

### **3 Experimental Design**

In this section, we describe the specific games included in our study and then provide a detailed description of our experimental procedures.

#### **3.1 The Games**

We choose four games which are variants of the six studied by Bednar and Page (2007). Here we test whether the phenomena derived within models and generated by artificial agents can be

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<sup>2</sup>A additional strand of research that complements our findings looks at the emergence of cooperation. Weber (2006) reports the results of a minimum-effort game experiment where successful coordination is achieved in large groups by starting with small groups and adding entrants who are aware of the group's history. Successful coordination in large groups can be interpreted as learning transfer from small groups that find it easier to coordinate.

produced in a laboratory with real people. We focus on four  $2 \times 2$  games: the Prisoner's Dilemma (PD), Strong Alternation (SA), Weak Alternation (WA), and a Self Interest game (SI).

The individual games belong to a class of two-person two-action games that contain a self-regarding action S and an alternative, C; in three of the games (PD, SA and WA), this alternative is cooperative. In these three games, cooperation lowers a player's own payoff and raises the payoff of the other and being selfish does the opposite, so in the one shot game, the unique dominant strategy equilibrium involves both players choosing selfish. In the fourth game, Self-Interest (SI), S is both the stage game dominant strategy and Pareto dominant.

The first game is a standard Prisoner's Dilemma, where the stage game has a dominant strategy equilibrium, (S, S), which is Pareto dominated by (C, C). Note that (C, C) also maximizes the joint payoff of the two players.

|                     |   |       |       |
|---------------------|---|-------|-------|
|                     |   | C     | S     |
| Prisoner's Dilemma: | C | 7, 7  | 2, 10 |
| (PD)                | S | 10, 2 | 4, 4  |

In the second and third games, Strong Alternation (SA) and Weak Alternation (WA), while (S, S) remains the dominant strategy equilibrium for the stage game, agents do best (i.e., maximize joint payoff) in repeated play by alternating between the off-diagonals, (C, S) and (S, C). In Strong Alternation, the incentives to alternate are much stronger than in Weak Alternation. The alternation games are a distant cousin to the conventional Battle of Sexes and Game of Chicken, where agents are rewarded for coordinating their behavior. In our alternation games, four outcomes are rewarded with positive payoffs: CC, SS, and the alternating strategies of CS then SC and SC then CS. Coordinating on CC or SS is much less taxing than working out an alternating behavior, and the positive payoffs for each reduce the focality of an alternating equilibrium.

|                     |   |       |       |
|---------------------|---|-------|-------|
|                     |   | C     | S     |
| Strong Alternation: | C | 7, 7  | 4, 14 |
| (SA)                | S | 14, 4 | 5, 5  |

|                   |   |       |       |
|-------------------|---|-------|-------|
|                   |   | C     | S     |
| Weak Alternation: | C | 7, 7  | 4, 11 |
| (WA)              | S | 11, 4 | 5, 5  |

In the final game, Self Interest (SI), the dominant strategy equilibrium, (S, S), also Pareto dominates all other outcomes. Furthermore, in the stage game, S uniformly dominates C.

|                |   |      |        |
|----------------|---|------|--------|
|                |   | C    | S      |
| Self Interest: | C | 7, 7 | 2, 9   |
| (SI)           | S | 9, 2 | 10, 10 |

### 3.2 Experimental Procedure

Our experiments consist of four control sessions, each of which consists of a single game, and 14 treatment sessions, each of which consists of a pair of games. This experimental design enables us to determine the effects of ensemble on behavior by comparing the ensemble with the corresponding control sessions and to compare behavior across ensembles.

The control sessions follow a common protocol for infinitely repeated games in the laboratory. We have one 12-player session for each of the single games. Participants are randomly matched into pairs at the beginning of each session, and play the same match for the entire experiment. In each session, participants first play the game for 200 rounds. After round 200, whether the game will continue to the next round depends on the “throw of the die” that is determined by the computer’s random number generator. At the end of each round after round 200, with 90% chance, the game will continue to the next round. With 10% chance, the game stops. In other words, we implement an infinitely repeated game, with a discount factor of 1 for the first 200 rounds, and 0.9 thereafter. With the chosen discount factors, (C, C) can be sustained as a repeated game equilibrium in PD, SA and WA. With 12 players in each control session, we have 6 independent observations for each single game.

In the ensemble treatment, we again use twelve players in each session. Within each session, at the beginning, each player is randomly matched with two other participants, both of whom will be her matches for the entire experiment. She plays two distinct games, one with each of her matches. For example, in the  $(PD_l, WA_r)$  ensemble, a player plays PD with her left match, and WA with her right match, as displayed in the following table using neutral action labels. This design allows us to analyze whether or not behavior in one game is influenced by the nature of the other game.

|        |            | Column Player |           |            |       | Column Player |           |
|--------|------------|---------------|-----------|------------|-------|---------------|-----------|
|        |            | Left (A)      | Right (B) |            |       | Left (A)      | Right (B) |
| Row    | Top (A)    | 7, 7          | 2, 10     | Top (A)    | 7, 7  | 4, 11         |           |
| Player | Bottom (B) | 10, 2         | 4, 4      | Bottom (B) | 11, 4 | 5, 5          |           |

As in the control sessions, we implement an infinitely repeated game, with a discount factor of 1 for the first 200 rounds, and 0.9 thereafter. Within each session, the twelve players are par-

tioned into independent groups of 4 each, yielding 3 independent observations. We number our players from one to twelve. The matching protocol is the following:  $\underbrace{4 - 2 - 1 - 3}$ ,  $\underbrace{6 - 5 - 7 - 8}$ ,  $\underbrace{10 - 9 - 11 - 12}$  form three independent groups, each with four participants positioned on a circle, and each participant plays her left and right match.

As the two games are displayed side by side, we conduct two independent sessions for each game ensemble, changing the order of the display to avoid the order effect within each round. For example, for the game ensemble of SA and WA, we display SA as the left game in one session, and WA as the left game in another session. This way, if a player always makes decisions from left to right, we have a balanced number of observations for each order.

We used z-Tree (Fischbacher 2007) to program our experiments. As z-Tree does not record the mouse movements within each stage, we ran two additional sessions with ensembles, (SI, WA) and (WA, SI), where we use the software Morae to record the mouse movement. These two sessions enable us to determine the order of decisions within each round. The (SI, WA) session has 12 subjects, while the (WA, SI) has only eight subjects.<sup>3</sup>

Table 1: Features of Experimental Sessions

| Control |    | Ensemble Treatment |               |         |        |
|---------|----|--------------------|---------------|---------|--------|
| Game    | n  | Pairs              | (Left, Right) | n       | Groups |
| PD      | 12 | 6                  | (PD, WA)      | 12      | 3      |
|         |    |                    | (WA, PD)      | 12      | 3      |
|         |    |                    | (PD, SI)      | 12      | 3      |
|         |    |                    | (SI, PD)      | 12      | 3      |
|         |    |                    | (SA, WA)      | 12      | 3      |
|         |    |                    | (WA, SA)      | 12      | 3      |
| SA      | 12 | 6                  | (SA, PD)      | 12      | 3      |
|         |    |                    | (PD, SA)      | 12      | 3      |
|         |    |                    | (SI, WA)      | 12 + 12 | 6      |
|         |    |                    | (WA, SI)      | 12 + 8  | 5      |
| SI      | 12 | 6                  | (SI, SA)      | 12      | 3      |
|         |    |                    | (SA, SI)      | 12      | 3      |
|         |    |                    | WA            | 12      | 6      |
| WA      | 12 | 6                  |               |         |        |
| Total   | 48 | 24                 |               | 164     | 41     |

Table 1 reports features of experimental sessions, including the name of the game, the number

<sup>3</sup>We recruited for twelve subjects, however, only eight showed up.

of players in each session, the number of independent pairs for each control session, the ensemble of games, the number of players in each session, as well as the number of independent groups in each ensemble session.

Overall, 18 independent computerized sessions were conducted in the RCGD lab at the University of Michigan from March to October 2007, yielding a total of 212 subjects. Our subjects were students from the University of Michigan, recruited by email from a subject pool for economic experiments.<sup>4</sup> Participants were allowed to participate in only one session. Each ensemble treatment session lasted approximately 90 minutes, whereas each control session lasted about 45 minutes. The exchange rate was set to 100 tokens for \$1. In addition, each participant was paid a \$5 show-up fee. Average earnings per participant were \$37.49 for those in the treatment sessions and \$22.77 for those in the control sessions. Data are available from the authors upon request.

## 4 Results: Control Sessions

In this section, we report the results from the control sessions at the outcome level. This analysis provides a benchmark from which we can identify the presence of cognitive load and behavioral spillovers results in Section 6. In Subsection 6.2, we infer the repeated game strategies emerged in each game in the control and compare them with those in the ensembles. In this section, we treat each pair as an independent observation.

We first introduce an empirical measure of cognitive load. To measure the behavioral variation in a game, we apply a standard entropy measure to the outcome distributions.<sup>5</sup> The *entropy* of a random variable  $X$  with a probability density function,  $p(x) = Pr\{X = x\}$ , is defined by

$$H(X) = - \sum_x p(x) \log_2 p(x),$$

Entropy measures the amount of stochastic variation in a random variable that can assume a finite set of values. Therefore it is also a measure of the amount of information required to describe that distribution. When using logarithms to base two, that measure captures the number of binary variables (bits) needed to describe the data.

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<sup>4</sup>Graduate students from the Economics Department are excluded from the list.

<sup>5</sup>Shannon (1948) is credited with the development of the concept of entropy and the birth of information theory. Many basic concepts and findings in this field are summarized in Cover and Thomas (2006).

For the analysis of two-person games, we model individual stage game strategies as a discrete random variable,  $X$ , with realizations in one of the four cells. Throughout the analysis, we use the convention that  $0 \log 0 = 0$ .<sup>6</sup> The entropy in a generic  $2 \times 2$  game is in the interval  $[0, 2]$ , with the lower bound indicating certainty, i.e., all outcomes are in one cell, and the upper bound indicating a uniform distribution among the four cells. The cause of behavioral variation could be strategic uncertainty over what the other player will do.

In Figures 1-4, we present time series data for each pair in each of the control sessions, with the entropy for each pair presented at the bottom of each graph.

[Figure 1 about here.]

Figure 1 presents outcomes in the Self Interest game. In this game, all six pairs converge to the Pareto dominant stage game equilibrium quickly and stay there. The entropy for each pair ranges from 0 to 0.04, indicating very little behavioral variation. This behavioral consistency is likely attributable to the uniform dominance property of the dominant strategy equilibrium in the stage game. Additionally, participants take an average of 0.62 seconds per round to make a decision in SI, significantly shorter than in any other game ( $p \leq 0.01$ , one-sided permutation tests). Based upon the uniform dominance property of the unique Pareto efficient stage game equilibrium, its low entropy, and response time, we posit that SI imposes the least cognitive load.

[Figure 2 about here.]

Figure 2 presents behavior in the Prisoner's Dilemma game. In this game, over half of the pairs play CC, the efficient outcome, which is consistent with findings from previous experiments (Andreoni and Miller 2002). Curiously, one pair also alternate for a fair number of rounds. The entropy for each pair ranges from 0.08 to 1.79, indicating changing behavioral variation. In addition, participants take an average of 1.00 second per round to make a decision in PD, significantly longer than SI, but shorter than SA ( $p \leq 0.01$ , one-sided permutation tests). As a "context" this game does not establish as strong a behavioral norm as the Self Interest game. Based upon this finding, we anticipate that PD will have a weaker behavioral pull than SI. The difficulty of learning to cooperate in the PD game may limit its spillover effects on play in other games.

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<sup>6</sup>This convention is easily justified by continuity, since  $x \log x \rightarrow 0$  as  $x \rightarrow 0$ .

[Figure 3 about here.]

Figure 3 presents behavior in the Strong Alternation game, where 5/6 of the pairs successfully establish the alternation outcomes. Pair 2 also attempts alternation on and off during the experiment. The entropy for each pair ranges from 1.29 to 1.90, indicating substantial behavioral variation.<sup>7</sup> In addition, participants take an average of 2.72 seconds per round to make a decision in SA, significantly longer than in any other game ( $p \leq 0.01$ , one-sided permutation tests). We interpret the longer response time in SA as evidence that coordinated alternation requires greater cognitive effort. Since successful alternation is established in five out of six pairs, this game also provides a strong context from which spillovers might occur.

[Figure 4 about here.]

Last, Figure 4 presents the dynamics from the Weak Alternation game. In this game, only two out of six pairs develop an alternating behavior, two pairs cooperate, one (pair 4) converges to SS, and the last pair (pair 6) does not seem to have converged to a stable outcome. The entropy for each pair ranges from 0.44 to 1.91, with the highest aggregate entropy among all four games. In addition, participants take an average of 1.24 seconds per round to make a decision in WA, significantly longer than SI, shorter than SA ( $p \leq 0.01$ , one-sided permutation tests), not significantly different from PD ( $p = 0.138$ , one-sided permutation test). As WA results in higher behavioral variation, we speculate that subject behavior in WA is more likely to be influenced by the other game in an ensemble.

Table 2: Distribution of Outcomes and Entropy in Control Sessions

|         | SI   |       | PD    |       | SA    |       | WA    |       |
|---------|------|-------|-------|-------|-------|-------|-------|-------|
|         | C    | S     | C     | S     | C     | S     | C     | S     |
| C       | 0.00 | 0.14  | 55.68 | 11.67 | 5.02  | 39.81 | 33.18 | 21.57 |
| S       | 0.00 | 99.86 | 14.82 | 17.82 | 40.37 | 14.81 | 22.74 | 22.51 |
| Entropy | 0.02 |       | 1.68  |       | 1.68  |       | 1.98  |       |

To summarize our findings, Table 2 reports the aggregate distribution of outcomes in each of the four games in the control sessions, and the respective entropy for each game in the last line. The

<sup>7</sup>Perfect coordinated alternation results in an entropy of 1.

behavioral variation measured by entropy is the lowest in the Self Interest game (0.02), followed by Prisoner’s Dilemma and Strong Alternation (1.68), and Weak Alternation (1.98). Using the entropy for each pair of players as an independent observation, we find that the ranking between SI and any other game is significant ( $p = 0.001$ , one-sided permutation tests) while other pairwise comparisons are not significant at the 10% level. Based on the entropy comparisons between games, we develop a partial ordering of the four games in terms of cognitive load:  $SI < PD \sim SA \sim WA$ . This partial ordering is consistent with that obtained from the response time comparisons, which has been used to measure cognitive activities in psychology (Luce 1986) and more recently, in behavioral economics (Rubinstein 2007). We postulate that games with lower entropy might have stronger behavioral spillovers than those with higher entropy.

In our outcome level analysis, we focus on the Pareto efficient outcomes: (1) for both players to always play selfish each round (SS) in the Self Interest game; (2) for both players to always cooperate (CC) in Prisoner’s Dilemma; and (3) coordinated alternation between S and C (ALT) in the Strong and Weak Alternation games, respectively. These outcomes also coincide with the simplest equilibria among the set of Pareto efficient ones in our set of games.<sup>8</sup>

Table 3: Average Proportion of Pareto Efficient Outcomes in Control Sessions

| Games | % Outcomes   |              |              | P-values of Permutation Tests |           |           |
|-------|--------------|--------------|--------------|-------------------------------|-----------|-----------|
|       | SS           | CC           | ALT          | CC v. SS                      | CC v. ALT | SS v. ALT |
| SI    | <b>99.86</b> | 0.00         | 0.00         | 0.000                         | 0.500     | 0.000     |
| PD    | 17.82        | <b>55.68</b> | 15.44        | 0.039                         | 0.031     | 0.389     |
| SA    | 14.81        | 5.02         | <b>71.12</b> | 0.040                         | 0.000     | 0.001     |
| WA    | 22.51        | 33.18        | <b>36.14</b> | 0.308                         | 0.430     | 0.317     |

Table 3 reports the proportion of three outcomes in each game over the entire series. Boldfaced numbers are the mode of the distribution. Within each game (row), we compare the proportion of pairs of outcomes, using one-sided permutation tests. The general null hypothesis is equal proportions, while the alternative hypothesis is that the proportion of the Pareto efficient outcome (boldfaced) is higher than any other outcome. The last three columns report the corresponding p-values for each pairwise test.

<sup>8</sup>When we represent a repeated game strategy as an automaton, the simplest strategy is defined as one with the least number of states (Kalai and Stanford 1988, Baron and Kalai 1993). We present our repeated game strategy analysis in Subsection 6.2.

In the control sessions, the proportion of Pareto efficient outcomes (SS in SI, CC in PD, ALT in SA and WA) is significantly higher than any other outcomes in SI, PD and SA ( $p < 0.05$ ). However, in WA, there is no significant difference in the proportions of any of the three outcomes ( $p > 0.10$ ).

In sum, three distinct outcomes emerge in the control sessions: in the SI game, selfishness; in the PD game, cooperation; and in SA and WA an alternating form of cooperation, where subjects alternate between the cooperative and selfish actions. Weak Alternation has weaker incentives, so the coordinated alternation is not as prominent as with Strong Alternation.

## 5 Hypotheses of Ensemble Effects

In this section, we present a set of hypotheses testing the null of game independence against our two posited ensemble effects, behavioral spillovers and cognitive load. Our alternative hypotheses, Hypothesis 1 - 6, are based on the theoretical results from Bednar and Page (2007), as well as our empirical results from the control sessions presented in Section 4. These hypotheses are also broadly consistent with the analogy based model of Jehiel (2005) and the case based reasoning of Gilboa and Schmeidler (1995).

Our general null hypothesis is of game independence: play in one game is not be affected by the existence of another game to play. If the independence hypothesis is correct then we should see no difference between behaviors in the control sessions (games played in isolation) and when games are presented to subjects as part of ensembles, nor should we see any difference in behavior in one game when it is paired with different games.

Based on results from Bednar and Page (2007), we anticipate that the ensemble play will depend upon *which* other game is in the ensemble. Since SI has significantly lower entropy than any of the three other games, we expect the dominant outcome in SI more likely to appear in the game it is paired with, but not vice versa. Specifically, we expect:

**Hypothesis 1** (Effects of SI). *Compared to the corresponding control or other ensembles, games paired with Self-Interest will exhibit more selfishness.*

Since pairwise entropy comparisons among PD, SA and WA are not significant, behavior in each game could influence or be influenced by the game it is paired with. We base the following

alternative hypotheses on other results from Bednar and Page (2007).

**Hypothesis 2** (Effects of PD). *Compared to the corresponding control or other ensembles, games (excluding SI) paired with the Prisoner's Dilemma will exhibit more cooperation.*

**Hypothesis 3** (Effects of SA). *Compared to the corresponding control or other ensembles, games (excluding SI) paired with Strong Alternation will exhibit more alternation.*

**Hypothesis 4** (Effects of WA). *Compared to the corresponding control or other ensembles, games (excluding SI) paired with Weak Alternation will exhibit more alternation.*

Payoff parameters for the two alternation games produce stronger incentives to alternate in Strong Alternation compared to Weak Alternation. This is confirmed by outcomes in the control sessions, with 71% (resp. 36%) of alternation in SA (resp. WA). Therefore, in ensembles, we expect to see more alternation in games paired with SA.

**Hypothesis 5** (Efficient Outcomes: Ensemble vs. Control). *Compared to the corresponding control sessions, subjects in a ensemble treatment will less often achieve efficient outcomes in any game with non-trivial entropy.*

Specifically, Hypothesis 5 implies that subjects in PD, SA or WA (each with non-trivial entropy) will less often produce efficient outcomes when each game is part of an ensemble compared to the corresponding control, while those in SI (with trivial entropy) will not behave differently in ensembles compared to the SI control.

In Section 4, we develop a partial ordering of the four games based upon the entropy of each game in the control sessions, i.e., the behavioral variation follows the order of  $SI < PD \sim SA \sim WA$ . Based on the entropy, response time and the payoff structure of each game, we posit that Self Interest is the only easy game to play so it will be the only game for which we do not expect to see a significant falloff in efficient outcomes in the game SI is paired with. Thus, we formulate a hypothesis based on the cognitive load of the context game.

**Hypothesis 6** (Efficient Outcomes: Ensemble vs. Ensemble). *Participants are more likely to achieve Pareto efficient outcomes in a game when it is paired with SI than when it is paired with other games.*

## 6 Results: Ensemble Effects

In this section, we present ensemble effects at the outcome level (subsection 6.1) as well as those at the strategy level (subsection 6.2). In all our analysis in this section, a pair in a control session or a group of four in an ensemble session is treated as an independent observation.

### 6.1 Ensemble Effects at the Outcome Level

Our anticipation was that subjects would play particular games differently between the control sessions, where they played a single game, and when that game appeared as part of an ensemble. This prediction emerges from the two core hypotheses: both behavioral spillovers and cognitive load will affect play in ensembles. Consequently, we expect different outcomes between the control sessions and the corresponding ensembles. To establish the existence of behavioral spillovers in the presences of cognitive load, we compare outcomes between ensembles.

Table 4: Distribution of Outcomes in the Control and Ensembles

|                | SI         |    |      | PD  |           |      | SA  |    |             | WA  |    |             |
|----------------|------------|----|------|-----|-----------|------|-----|----|-------------|-----|----|-------------|
|                | (SS        | CC | ALT) | (SS | CC        | ALT) | (SS | CC | ALT)        | (SS | CC | ALT)        |
| SI paired with | <b>100</b> | 0  | 0)   | (99 | 0         | 0)   | (99 | 0  | 0)          | (99 | 0  | 0)          |
| PD paired with | (46        | 42 | 5)   | (18 | <b>56</b> | 15)  | (23 | 41 | 21)         | (39 | 40 | 9)          |
| SA paired with | (32        | 7  | 48)  | (24 | 15        | 48)  | (15 | 5  | <b>71</b> ) | (39 | 10 | 38)         |
| WA paired with | (28        | 44 | 21)  | (40 | 31        | 18)  | (40 | 11 | 37)         | (23 | 33 | <b>36</b> ) |

*Note:* The diagonal is the outcome distribution for the control sessions.

Boldfaced numbers are the mode of distribution for the control sessions.

Table 4 presents the outcome distribution for the control and ensemble treatments. Each cell contains the proportion of SS, CC and ALT for the row game, when it is paired with the column game. The dominant diagonal contains the outcome distribution for the control sessions. We can then test Hypotheses 1 to 4 using information in this table. For example, Hypothesis 1 predicts that, row-by-row (excluding the SI row), the proportion of SS is largest when a game is paired with SI. In what follows, we present the results testing each hypothesis and tabulate the statistical support in a separate table for each hypothesis.

**Result 1** (Effects of SI). *The proportion of SS in PD is weakly higher when it is paired with SI (46%) than when it is played in isolation (18%) or when it is paired with SA (23%). Similarly, the proportion of SS in SA is weakly higher when it is paired with SI (32%) than when it is played in isolation (15%). The latter becomes significant after Round 100 (32% versus 6%).*

**Support.** *In Table 4, pairwise comparisons between the SS columns represent the effects of SI on the likelihood of selfishness in other games. Permutation tests of the general null hypothesis of game independence against Hypothesis 1 are reported in Table 5 below. After Round 100, the difference between (SA, SI) and SA control becomes significant ( $p = 0.031$ , one-sided permutation test).*

Table 5: Effects of SI on Other Games: Permutation Tests

|                  |                     |                     |                     |
|------------------|---------------------|---------------------|---------------------|
| SS in<br>(PD,SI) | PD control<br>0.070 | (PD,SA)<br>0.109    | (PD,WA)<br>0.371    |
| (SA,SI)          | (SA,PD)<br>0.290    | SA control<br>0.065 | (SA,WA)<br>0.680    |
| (WA,SI)          | (WA,PD)<br>0.846    | (WA,SA)<br>0.813    | WA control<br>0.364 |

By Result 1, we reject the null in favor of Hypothesis 1 at the 10% level for two sets of comparisons. When paired with SI, the proportion of SS is larger for PD (resp. SA) than when it is played in isolation or when it is paired with SA (resp. PD). After 100 rounds, one set of comparison is significant at the 5% level. We also note that SI does not have such an effect on WA.

We now examine the effects of PD on other games. Hypothesis 2 predicts that, in Table 4, row-by-row (excluding the PD row), the proportion of CC is largest when a game is paired with PD. While the outcome distribution of SI is not affected by any game it is paired with, the effects of PD on cooperation is present in SA, and to a lesser extent, in WA.

**Result 2** (Effects of PD). *Comparing (SA, PD) and SA control sessions, the proportion of CC is significantly higher when SA is paired with PD (15% versus 5%). Comparing (SA, PD) and (SA, SI), we observe CC more often in SA when paired with PD (15% versus 7%). The difference is more pronounced and significant after Round 100 (14% versus 1%).*

Similarly, comparing (WA, PD) and (WA, SA), the proportion of CC is significantly higher when WA is paired with PD (31% versus 11%).

**Support.** In Table 4, pairwise comparisons between the CC columns when a game is paired with PD versus when it is paired with another game represent the effects of PD on the likelihood of CC in other games. One-sided permutation tests of the general null hypothesis of game independence against Hypothesis 2 are reported in Table 6. One-sided permutation test comparing the proportion of CC in SA in ensembles (SA, PD) and (SA, SI) yields  $p = 0.023$  after 100 rounds.

Table 6: Effects of PD on Other Games: Permutation Tests

|                  |                     |                     |                     |
|------------------|---------------------|---------------------|---------------------|
| CC in<br>(SI,PD) | SI control<br>1.000 | (SI,SA)<br>1.000    | (SI,WA)<br>1.000    |
| (SA,PD)          | (SA,SI)<br>0.119    | SA control<br>0.049 | (SA,WA)<br>0.299    |
| (WA,PD)          | (WA,SI)<br>0.897    | (WA,SA)<br>0.024    | WA control<br>0.566 |

By Result 2, we reject the general null hypothesis in favor of Hypothesis 2 for the effects of PD on SA and WA for some ensemble comparisons. However, PD has no effect on SI.

**Result 3 (Effects of SA).** When PD (resp. WA) is paired with SA, the proportion of ALT is larger than when it is played in isolation or when it is paired with any other game. However, none of the pairwise comparisons is significant.

**Support.** In Table 4, pairwise comparisons between the ALT columns when a game is paired with SA versus when it is paired with another game represent the effects of SA on the likelihood of ALT in other games. One-sided permutation tests of the general null hypothesis of game independence against Hypothesis 3 are reported in Table 7.

By Result 3, we fail to reject the general null hypothesis in favor of Hypothesis 3. Although the proportion of ALT is the largest when a game is paired with SA than when it is played in isolation or when it is paired with any other game, Hypothesis 4 is not supported in our data.<sup>9</sup>

<sup>9</sup>We omit the table reporting p-values of the corresponding pairwise one-sided permutation tests, none of which is significant at the 10% level.

Table 7: Effects of SA on Other Games: Permutation Tests

|                   |                     |                     |                     |
|-------------------|---------------------|---------------------|---------------------|
| ALT in<br>(SI,SA) | SI control<br>1.000 | (SI,PD)<br>1.000    | (SI,WA)<br>0.647    |
| (PD,SA)           | (PD,SI)<br>0.110    | PD control<br>0.355 | (PD,WA)<br>0.183    |
| (WA,SA)           | (WA,SI)<br>0.142    | (WA,PD)<br>0.119    | WA control<br>0.485 |

Although WA does not have any effects on the likelihood of alternation on other games as hypothesized, it has an unexpected effect on selfish play in PD and SA. When PD is paired with WA, SS is nearly as often as when PD was paired with SI; for SA, the effect of pairing SA and WA is even greater than with SA and SI.

**Result 4** (Effects of WA). *The proportion of SS is significantly higher in (PD, WA) (39%) than in the PD control sessions (18%) or in (PD, SA) (23%). Likewise, the proportion of SS is significantly higher in (SA, WA) (39%) than in the SA control sessions (15%).*

**Support.** *Pairwise comparisons between the SS columns when a game is paired with WA versus when it is paired with another game in Table 4 indicate the effects of WA on the likelihood of selfishness in other games. Permutation tests of the general null hypothesis of game independence against the hypothesis of higher SS in a game when it is paired with WA are reported in Table 8.*

Table 8: Effects of WA on Other Games: Permutation Tests

|                  |                     |                     |                     |
|------------------|---------------------|---------------------|---------------------|
| SS in<br>(SI,WA) | SI control<br>0.997 | (SI,PD)<br>0.695    | (SI,SA)<br>0.630    |
| (PD,WA)          | (PD,SI)<br>0.630    | PD control<br>0.030 | (PD,SA)<br>0.036    |
| (SA,WA)          | (SA,SI)<br>0.321    | (SA,PD)<br>0.174    | SA control<br>0.043 |

We conjecture that the increase of SS in PD (resp. SA) when it is paired with WA might be due to increased cognitive load, as WA played in isolation has the highest entropy among the four games. Thus, when either PD or SA is played with WA, subjects might resort to the dominant strategy in the stage game when they play PD and SA.

We now turn to Hypothesis 5 where we aggregate the previous analysis by comparing Pareto efficient outcomes in the control and ensembles. In the control sessions, the Pareto-efficient outcomes (SS in SI, CC in PD, ALT in SA and WA) emerge as the mode among all the three outcomes in SI, PD and SA played in isolation (diagonal in Table 4).

Table 9: Pareto Efficient Outcomes in Ensemble vs. Control

|  | SS in SI | CC in PD | ALT in SA | ALT in WA |
|--|----------|----------|-----------|-----------|
| % in Control                                     | 0.999    | 0.557    | 0.711     | 0.361     |
| % in Ensemble                                    | 0.991    | 0.410    | 0.449     | 0.244     |
| $H_1$ : control > ensemble<br>one-sided p-values | 0.002    | 0.171    | 0.031     | 0.213     |
| # of observations<br>(control, ensemble)         | (6, 23)  | (6, 18)  | (6, 18)   | (6, 23)   |

*Note:* In the permutation tests, we treat each pair (group of four) in the control (ensemble) sessions as one observation.

Table 9 reports the proportion of Pareto efficient outcomes in the control and ensembles, as well as p-values from one-sided permutation tests. The general null hypothesis is game independence, i.e., the proportion of Pareto efficient outcomes of a particular game is the same between the control and ensemble treatments, while the alternative hypothesis is that the the proportion of Pareto efficient outcomes is higher when a game is played alone. We summarize the results below.

**Result 5** (Pareto Efficient Outcomes in Ensembles). *In every game, the proportion of the Pareto efficient outcome decreases when a game is part of an ensemble than when the same game is played in isolation. This decrease is significant for ALT in SA.*

**Support.** *In Table 9, we reject the null of game independence in favor of  $H_1$  for SS in SI ( $p = 0.002$ ), and ALT in SA ( $p = 0.031$ ).*

Result 5 indicates a general decrease of Pareto efficient outcomes when a game is played in an ensemble compared to the same game played in isolation. In particular, in Strong Alternation, subjects alternate significantly less ( $p = 0.031$ ) when it is in an ensemble than when it is played in isolation. The Self Interest game, however, is not affected by the presence of other games. It is the easiest game to play. Whether in control or ensemble treatments, subjects quickly converge to

SS, with over 99% of selfishness across the rounds. Thus, by Result 5, we reject the null of game independence in favor of Hypothesis 5 in SA.

Lastly, we examine Hypothesis 6 which postulates that the proportion of Pareto efficient outcomes in a game is higher when it is paired with SI than when it is paired WA. While this hypothesis correctly forecasts the direction of change, none of the pairwise comparisons is significant at the 10% level.

We next compare the efficiency generated in each game. Following convention, we capture efficiency by the percentage of potential payoff above the minimum payoff that the players receive. Our normalized efficiency measure is defined as follows.

$$\text{Efficiency} = \frac{\text{Actual joint payoffs} - \text{Minimum joint payoffs}}{\text{Maximum joint payoffs} - \text{Minimum joint payoffs}} \quad (1)$$

Table 10: Efficiency in the Control and Ensembles

|                | SI           | PD           | SA           | WA           |
|----------------|--------------|--------------|--------------|--------------|
| SI paired with | <b>99.86</b> | 99.32        | 99.23        | 98.99        |
| PD paired with | 51.5         | <b>73.35</b> | 63.59        | 53.97        |
| SA paired with | 64.24        | 68.1         | <b>82.69</b> | 55.66        |
| WA paired with | 63.06        | 53.97        | 57.89        | <b>70.86</b> |

Table 10 presents the average efficiency in the control and the ensemble sessions. In each row, we present the efficiency of the row game when it is played alone (diagonal, boldfaced) and when it is paired with another game. Consistent with outcome level results, the efficiency in SI, PD and SA control sessions is higher than that of the corresponding games in ensemble sessions. In particular, the following comparisons, **SI** > (**SI**, SA), **SI** > (**SI**, WA), and **SA** > (**SA**, WA), are significant at the 5% level, while **SA** > (**SA**, SI) and **SA** > (**SA**, PD) are significant at the 10% level (see Table 11 for p-values of one-sided permutation tests).

Table 12 reports the p-values of one-sided permutation tests of pairwise efficiency comparisons of a common game when it is paired with different games. None of the pairwise comparisons is significant at the 10% level.

In general, the experimental results agree with our alternative hypotheses: game independence is not supported, but instead subjects are influenced by contextual effects of behavioral spillovers

Table 11: Efficiency Comparison between Control and Ensemble: Permutation Tests

| Control | (SI,PD) | (SI,SA) | (SI,WA) |
|---------|---------|---------|---------|
| SI      | 0.130   | 0.002   | 0.004   |
|         | (PD,SI) | (PD,SA) | (PD,WA) |
| PD      | 0.120   | 0.225   | 0.066   |
|         | (SA,SI) | (SA,PD) | (SA,WA) |
| SA      | 0.052   | 0.099   | 0.034   |
|         | (WA,SI) | (WA,PD) | (WA,SA) |
| WA      | 0.290   | 0.134   | 0.217   |

Table 12: Efficiency Comparison between Ensembles: Permutation Test Results

| Game in | Game Ensemble |         |         | P-Values of Permutation Tests |             |             |
|---------|---------------|---------|---------|-------------------------------|-------------|-------------|
|         | (1)           | (2)     | (3)     | (1) vs. (2)                   | (1) vs. (3) | (2) vs. (3) |
| PD in   | (PD,SA)       | (PD,SI) | (PD,WA) | 0.240                         | 0.170       | 0.428       |
| SA in   | (SA,PD)       | (SA,SI) | (SA,WA) | 0.387                         | 0.185       | 0.273       |
| WA in   | (WA,PD)       | (WA,SI) | (WA,SA) | 0.191                         | 0.371       | 0.335       |
| SI in   | (SI,PD)       | (SI,SA) | (SI,WA) | 0.411                         | 0.341       | 0.417       |

and cognitive load. While analyses reported in this subsection are based on non-parametric tests, we recognize that income effects might influence behavior. Thus, we use probit regressions with standard errors clustered at the pair (respectively group) level for Results 1 to 5, controlling for income and learning effects in each specification. Following Ham, Kagel and Lehrer (2005), we use a participant’s cash balance prior to period  $t$  to control for income effects. We find that, while cash balance is statistically significant in most specifications, its marginal effect on behavior is never greater than 1%.<sup>10</sup> Further, Results 1 to 5 continue to hold in our regression analysis.

## 6.2 Ensemble Effects at the Strategy Level

In this subsection, we analyze repeated game strategies in each game, and the ensemble effects at the strategy level. Following Rubinstein (1986) and Abreu and Rubinstein (1988), we use automaton (or the Moore machine) to represent repeated game strategies. In Figure 5, we present 29 repeated game strategies, including the exhaustive set of 26 1- and 2-state automata, and three 3-, 4- and 5-state automata which have been widely discussed in previous literature (Engle-Warnick and

<sup>10</sup>Regression tables are available from the authors upon requests.

Slonim 2006). For each subject  $i$ , we calculate the *fitting proportion* for each automaton,  $M_j$ , for the entire sequence of observed actions  $\{a_i^t\}_{t=1}^T$ , defined as  $F_i(M_j) = \sum_{t=1}^T I(a_i^t, M_j^t)/T$ , where the indicator function  $I(a_i^t, M_j^t) = 1$  if  $a_i^t = M_j^t$ . At the treatment level, we define the average fitting proportion as  $\bar{F}(M_j) = \sum_{i=1}^n F_i(M_j)/n$ , where  $n$  is the number of players.

To highlight the main results, in subsequent discussions, we only compare the performance of a subset of 1- and 2-state automata.<sup>11</sup> Table 13 presents 9 out of 26 1- and 2-state automata, including all six strategies with at least 50% fitting proportion across all games and ensembles, and three which do not survive the 50% fitting threshold but have been extensively discussed in the literature (Engle-Warnick and Slonim 2001; Bednar and Page 2007; Hanaki et al. 2005). These 9 strategies can be divided into three categories: (1) cooperative strategies, including Always Cooperate (AC), Forgive Once (F1), Suspicious Forgive Once (sF1); (2) reciprocal strategies, including Tit-for-Tat (TFT), and Suspicious Tit-for-Tat (sTFT); and (3) selfish strategies, including Always Selfish (AS), Grim Trigger (GT),<sup>12</sup> Switch after Cooperate (SAC), suspicious Switch after Cooperate (sSAC). Of these nine strategies, AC, AS and GT do not survive the 50% fitting threshold.

The strategy level analysis in the control sessions reveals few surprises. In the PD game, reciprocal strategies, TFT and sTFT, have significantly higher fitting proportion,  $\bar{F}(TFT) = \bar{F}(sTFT) = 0.84$ , than every other strategy.<sup>13</sup> This result is consistent with the literature where TFT is widely and successfully used in the repeated PD simulations (Axelrod and Hamilton 1981, Bednar and Page 2007, Hanaki et al 2005). These two strategies have even better fitting proportion,  $\bar{F}(TFT) = \bar{F}(sTFT) = 0.90$ , in the Weak Alternation game.<sup>14</sup> In the Strong Alternation game, TFT, sTFT as well as SAC and sSAC are all best fitting strategies, each with a fitting proportion of  $\bar{F} = 0.85$ , and each significantly outperforming every other strategy outside this set.<sup>15</sup> This

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<sup>11</sup>The complete analysis of all 29 automata are available from the authors upon request.

<sup>12</sup>We classify GT as a selfish strategy because, when faced with any match that plays S with some positive probability, GT is identical to AS from then on. However, we recognize that it is subgame perfect punishment. Further, GT-GT is a subgame perfect equilibrium which achieves perfect cooperation. Thus, this classification is not perfect.

<sup>13</sup> $\bar{F}(TFT) > \bar{F}(M_j)$ :  $p < 0.05$  for any  $M_j \neq \{AC, sTFT\}$ , and  $p < 0.10$  for  $M_j = AC$ . Similarly,  $\bar{F}(sTFT) > \bar{F}(M_j)$ :  $p < 0.05$  for any  $M_j \neq \{sF1, AC, TFT\}$ , and  $p < 0.10$  for  $M_j \in \{sF1, AC\}$ , one-sided Wilcoxon signed rank tests.

<sup>14</sup> $\bar{F}(TFT) > \bar{F}(M_j)$ :  $p < 0.05$  for any  $M_j \neq \{SAC, sSAC, sTFT\}$ , and  $p < 0.10$  for  $M_j \in \{SAC, sSAC\}$ . Similarly,  $\bar{F}(sTFT) > \bar{F}(M_j)$ :  $p < 0.05$  for any  $M_j \neq \{F1, SAC, sSAC, TFT\}$ , and  $p < 0.10$  for  $M_j \in \{F1, SAC, sSAC\}$ , one-sided Wilcoxon signed rank tests.

<sup>15</sup>SAC or sSAC has significantly greater fitting proportion than any other strategy outside the set ( $p < 0.05$ ), while TFT or sTFT has significantly greater fitting proportion than any other strategy outside the set ( $p < 0.05$ ) except for F1 ( $p < 0.10$ ), one-sided Wilcoxon signed rank tests.

Table 13: Description of Nine Strategies

| Strategy Category | Name of Strategy                | Strategy Number | Initial Action | Continued Play   |
|-------------------|---------------------------------|-----------------|----------------|--|
| Cooperative       | Always Cooperate (AC)           | M1              | C              | Always play cooperate  |
|                   | Forgive once (F1)               | M8              | C              | Go to S if other plays S and go to C when the last period is S |
|                   | Suspicious Forgive once(sF1)    | M9              | S              | Go to S if other plays S and go to C when the last period is S |
| Reciprocal        | Tit for Tat (TFT)               | M4              | C              | Copy other's previous action                                   |
|                   | Suspicious Tift For Tat (sTFT)  | M5              | S              | Copy other's previous action                                   |
| Selfish           | Always Selfish (AS)             | M2              | S              | Always play selfish  |
|                   | Grim Trigger (GT)               | M3              | C              | C until other plays S, then S forever                          |
|                   | Switch After C(SAC)             | M6              | C              | After C, play S until other plays C                            |
|                   | Suspicious Switch After C(sSAC) | M7              | S              | After C, play S until other plays C                            |

result is consistent with Hanaki et al (2005) where in a simulation of coordination games similar to Strong Alternation, SAC is the best performing strategy. Finally, in the Self Interest game, due to the lack of variation in actions, player behavior can be explained by any different strategy that produces all selfish behavior. Among these strategies are TFT, sTFT, SAC, sSAC, AS, and GT, each has a fitting proportion of  $F = 1.00$ .

The strategy level analysis for the ensemble sessions also aligns with expectations. Comparing strategies used in PD when it is paired with SI and those used in the PD control sessions, we find that the fitting proportion of selfish strategies increases from control to ensembles. For example, the fitting proportion of strategies that choose to be selfish after cooperating (SAC and sSAC) increases from 0.59 in the control to 0.71 in the ensemble ( $p = 0.08$ , one-sided permutation test). It is still the case though that TFT and sTFT retain the greatest fitting proportion in PD ( $\bar{F} = 0.91$ ) even when it is paired with SI. Likewise, when PD is paired with WA, the fitting proportion of selfish strategies again increases, with  $\bar{F}(AS) = 0.31$  in the control sessions and 0.49 in the (PD, WA) ensemble ( $p = 0.09$ ),  $\bar{F}(SAC) = 0.59$  in the control and 0.66 in the ensemble ( $p = 0.06$ ), and  $\bar{F}(sSAC) = 0.59$  in the control and 0.66 in the ensemble ( $p = 0.07$ ).

Comparing strategies used in SA when it is paired with SI and those used in the SA control sessions, we find that the fitting proportion of selfish strategies significantly increases from the control to the ensemble, while that of cooperative strategies weakly decreases. Specifically,  $\bar{F}(GT) = 0.55$  in the control and 0.65 in the ensemble ( $p = 0.02$ ), while  $\bar{F}(AC) = 0.45$  in the control and 0.37 in the ensemble ( $p = 0.10$ ). We obtain similar results comparing the (SA, WA) ensemble and SA control sessions.

Last, when we compare repeated game strategies between ensembles, several of the results from the outcome level analysis survive, albeit in a slightly different form. Specifically, we find behavioral spillover effects of PD and SA, as well as cognitive load effects.

Consistent with Result 2 where the proportion of CC is higher when a game is paired with PD, we find that, in the (WA, PD) vs.(WA, SA) ensembles, when WA is paired with PD, the fitting proportion of cooperative strategies, such as always cooperate (AC), is weakly higher than when it is paired with SA (45 vs. 36%,  $p = 0.10$ ), while that of selfish strategies, such as AS (55 vs. 64%), GT (55 vs. 64%), SAC (72 vs. 81%) and sSAC (72 vs. 81%) is weakly higher when WA is paired with SA ( $p < 0.1$  for each comparison, one-sided permutation tests). Likewise, when SA is paired

with PD, the fitting proportion of cooperative strategies including AC, F1 and sF1 is higher than when it is paired with SI or WA, however, none of these pairwise comparison is significant at 10% level.

Consistent with Result 3 where the proportion of ALT is higher when a game is paired with SA, we find that, in the (WA, SA) vs.(WA, SI) ensembles, when WA is paired with SA, the fitting proportion of SAC (sSAC) in WA is significantly higher than when it is paired with SI (SAC: 81 vs. 71%,  $p = 0.033$ ; sSAC: 81 vs. 71%,  $p = 0.035$ , one-sided permutation tests).

While Hypothesis 6 on cognitive load is only supported directionally at the outcome level, we find statistically significant effects at the strategy level. Comparing PD strategies in the (PD, SI) vs. (PD, WA) ensembles, when PD is paired with SI, the fitting proportion of TFT and sTFT is significantly higher than when it is paired with WA (TFT: 91 vs. 83%,  $p = 0.039$ ; sTFT: 91 vs. 83%,  $p = 0.042$ , one-sided permutation tests).

In sum, analysis of behavioral spillovers at both the outcome and strategy levels yields largely consistent results, i.e., when games are paired in ensembles, play differs from isolated controls, and in predictable ways. In some cases, the two levels of analysis provide different lenses on the same phenomenon. For example, both analyses demonstrate that a game paired with the PD game exhibits more cooperative outcomes and strategies than observed in the control or when it is paired with another game. In other cases, the strategy level analysis highlights a different feature of the results. For example, the strategy analysis allows us to see how often pairs are able to coordinate on alternating strategies.

## 7 Discussion

In this paper, we present an experimental study to test for ensemble effects in game playing behavior. We test for these effects looking both at outcomes and strategies. Our study reveals evidence of behavioral spillovers that depend in predictable ways on features of the games in the ensemble. In particular, if subjects play one game in an ensemble that encourages selfishness or cooperation, then they are more likely to exhibit that behavior in the other game in their ensemble, even though they play the other game with a different player. We also see evidence of cognitive load.

To derive our hypotheses about cognitive load and behavioral spillovers, we introduce a new

measure of behavioral variance, *entropy*, which is consistent with response time, an alternative measure of cognitive load used in psychology. We compute the entropy of a game played in isolation and make *out-of-sample* predictions of its effect in game ensembles. We posit that in ensembles that include games that produce high entropy outcomes, cognitive load will be most pronounced. Consistent with our expectations, cognitive load has the greatest effect when ensembles include Weak Alternation, our highest-entropy game. In contrast, we hypothesize that low entropy games would produce stronger behavioral spillovers and are less influenced by other games. Both predictions are supported by our data.

Our findings provide an initial demonstration of how a person's behavior in a given game depends on the ensemble of strategic situations that the person faces. In doing so, they call into question the focus on isolated games in most theoretical and empirical analyses. This critique extends to mechanism design, which assumes that incentives can be considered independent of the broader behavioral context.

To summarize, our multiple games experiments demonstrate that significant ensemble effects emerge in the laboratory setting. Outcome level and strategy level analysis show consistent ensemble effects. Subjects with incentives to behave cooperatively (resp. selfishly) in one game, tend to behave similarly in another game even if that behavior is not efficient. Similar behavioral spillovers are observed in other ensemble experiments using more complex games, such as the public goods game and lottery contest (Savikhin and Sheremeta 2010), the median- and minimum-effort games (Cason et al. 2010), and the threshold public goods and double auctions (Cason and Gangadharan 2010). This emerging literature indicates that contexts affect behavior.

## Appendix. Experimental Instructions

*We present the instructions for the (PD, WA) ensemble. Instructions for other ensemble treatments are identical except for the specific game forms. Instructions for the control sessions are identical to the ensemble instructions except that two games and two other participants are replaced with one game and one other participant everywhere. Hence we omit them here.*

Name:

PCLAB:

Total Payoff:

### Introduction

- You are about to participate in a decision process in which you will play two games with two other participants. Each game will be played with a different participant and will be played for many rounds. This is part of a study intended to provide insight into certain features of decision processes. If you follow the instructions carefully and make good decisions, you may earn a considerable amount of money. You will be paid in cash at the end of the experiment.
- During the experiment, we ask that you please do not talk to each other. If you have a question, please raise your hand and an experimenter will assist you.

### Procedure

- Matching: At the beginning of the experiment, you will be matched randomly with two other participants, both of whom will be your matches for the entire experiment. You will be matched with these same two people in all rounds. You will play a different game with each of these people.
- Roles: Throughout the game, you will be designated as the “row” player and your matches will be the “column” players. You will be a “row” player in all rounds, and your matches will be “column” players in all rounds
- Actions: In each round, you and your two matches will simultaneously and independently make decisions in two different games. One is the left game and the other is the right game.

You will play the left game with one of your matches (Left Game Match) and play the right game with the other match (Right Game Match). In each game, the row player (you) will click either the Top (A) or the Bottom (B) button. The column player (your Left or Right Game Match) will choose either the Left (A) or Right (B) button. These choices determine which part of the matrix is relevant (Top Left, Top Right, Bottom Left, Bottom Right).

- Interdependence: A player's earnings depend on the decision made by the player and on the decision made by his or her two matches as shown in the matrix below. In each cell, the row player's payoff is shown in red and the column player's payoff is shown in blue.

|            |            | Column Player |           |            |       | Column Player |           |
|------------|------------|---------------|-----------|------------|-------|---------------|-----------|
|            |            | Left (A)      | Right (B) |            |       | Left (A)      | Right (B) |
| Row Player | Top (A)    | 7, 7          | 2, 10     | Top (A)    | 7, 7  | 4, 11         |           |
|            | Bottom (B) | 10, 2         | 4, 4      | Bottom (B) | 11, 4 | 5, 5          |           |

For example, if the row player (you) chooses Top (A) and the column player (your left game match) chooses Right (B) in the left game, then the row player (you) will get 2 points, while the column player (your left game match) will get 10 points in this game. Meanwhile, if the row player (you) chooses Bottom (B) and the column player (your right game match) chooses right (B) in the right game, then the row player (you) will get 5 points, and the column player (your right game match) will also get 5 points in this game. So as the row player in both games, you will get 7 points in this round totally.

- Rounds: You will first play the two games for 200 rounds. After round 200, whether the games will continue to the next round depends on the "throw of a die" that is determined by the computer's random number generator. At the end of each round after round 200, with 90% chance, the games will continue to the next round. With 10% chance, the games stop.
- Earnings: Your earnings are determined by the choices that you and your two matches make in every round. Your total earning is the sum of your earnings in all rounds.

The exchange rate is \$1 for 100 points.

You can round up your total earning to the next dollar. For example, if you earn \$15.23, you can round it up to \$16.

- History: In each round, your and your two matches' decisions in all previous rounds will be displayed in a history window.

We encourage you to earn as much money as you can. Do you have any questions?



Figure 1: Control: Behavior in Self Interest

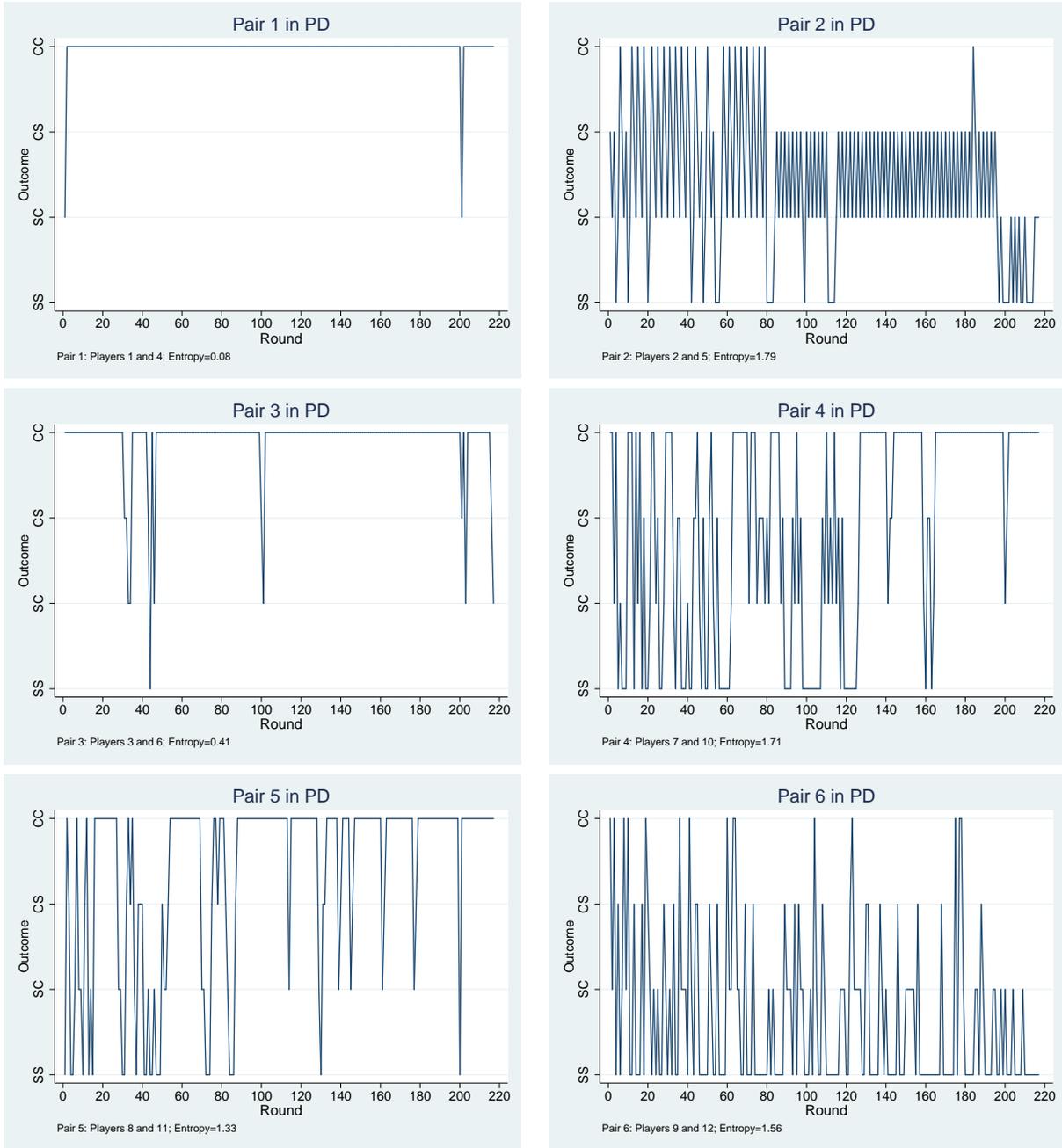


Figure 2: Control: Behavior in Prisoner's Dilemma

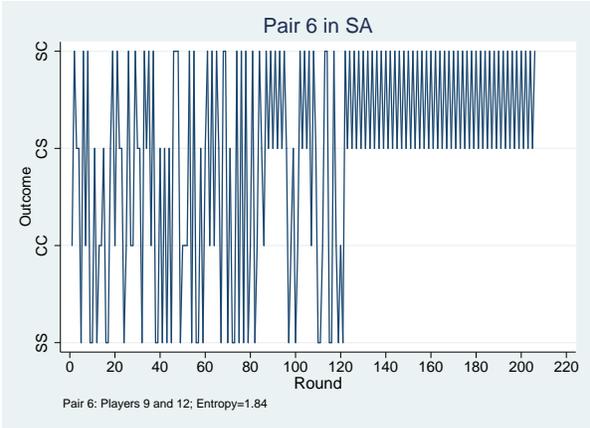
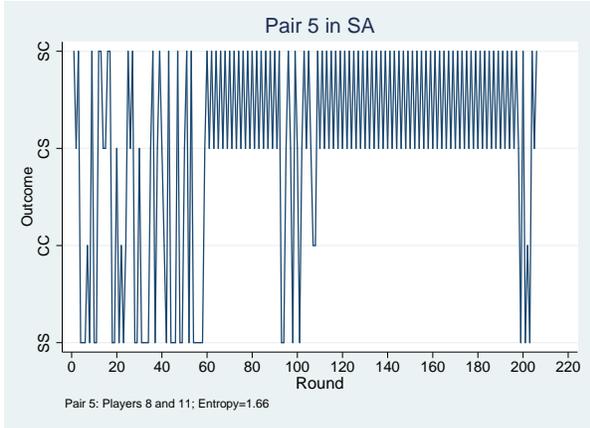
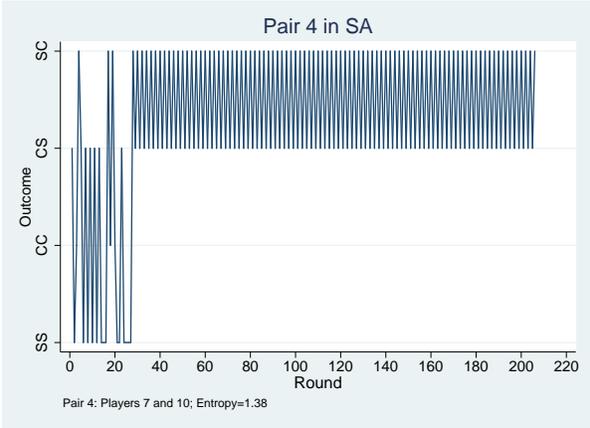
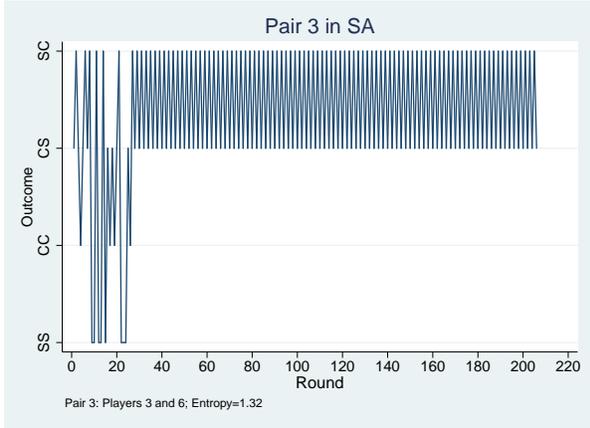
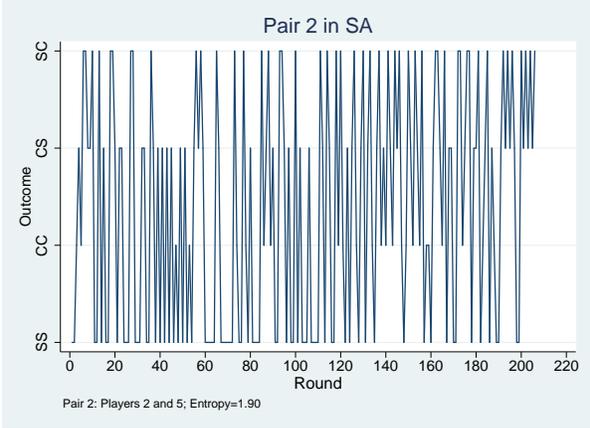
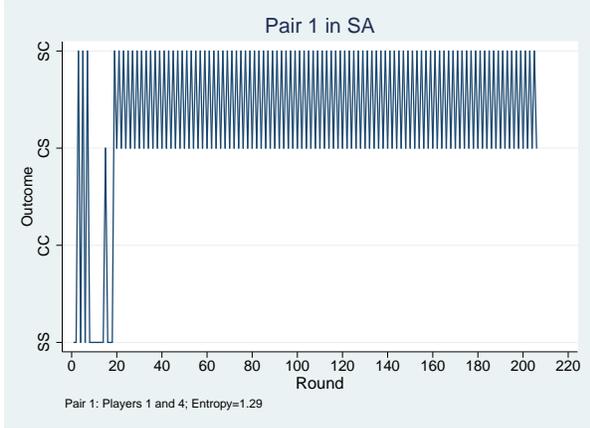


Figure 3: Control: Behavior in Strong Alternation

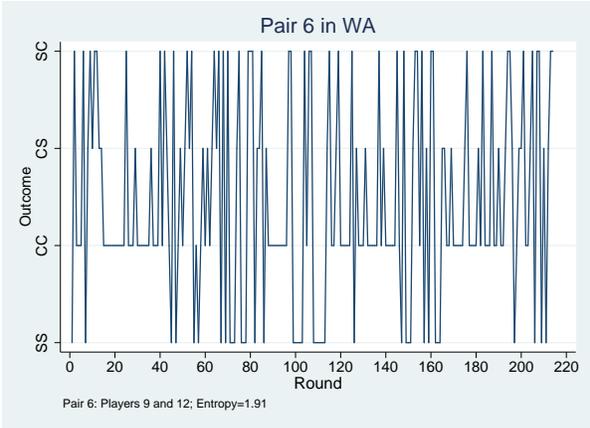
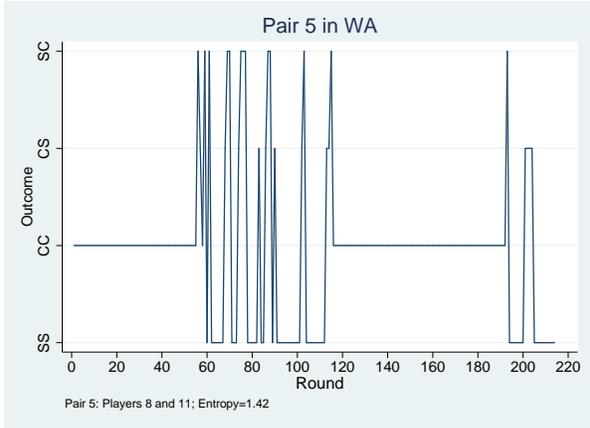
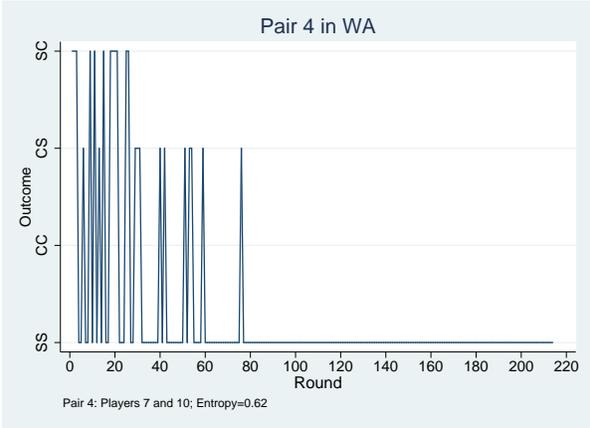
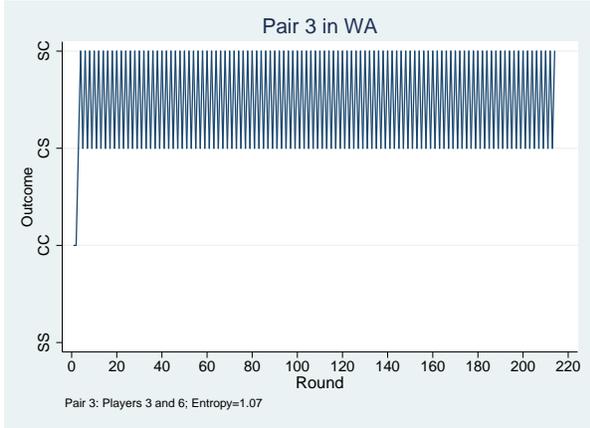
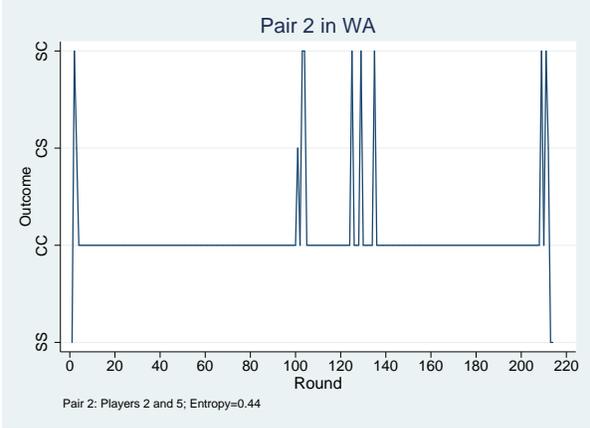
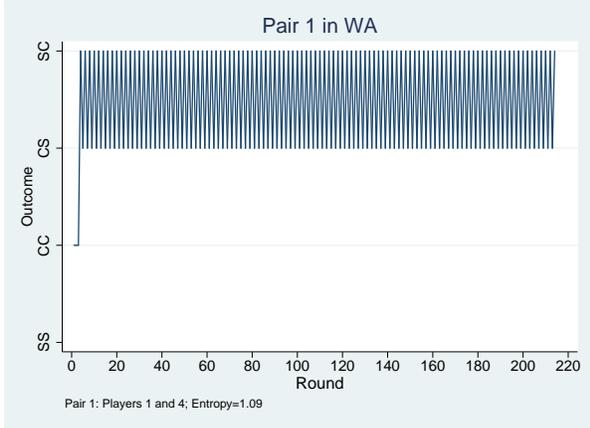
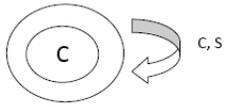
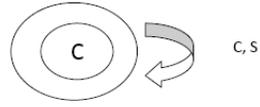


Figure 4: Control: Behavior in Weak Alternation

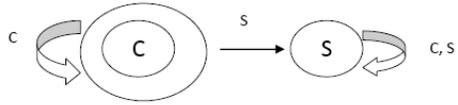
M1 (AC)



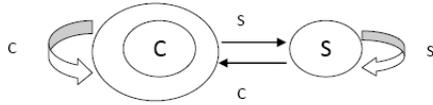
M2 (AS)



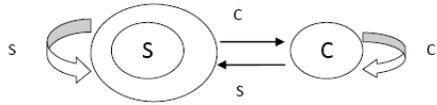
M3 (GT)



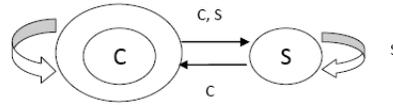
M4 (TFT)



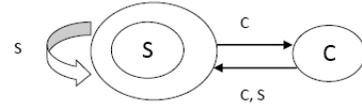
M5 (sTFT)



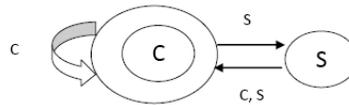
M6 (SAC)



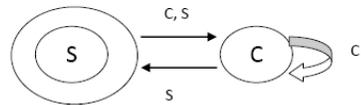
M7 (sSAC)



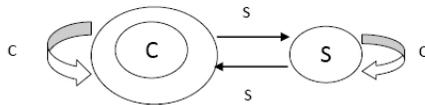
M8 (F1)



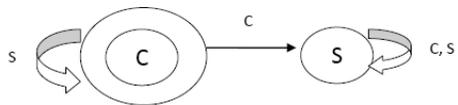
M9 (sF1)



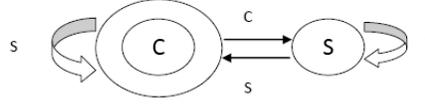
M10



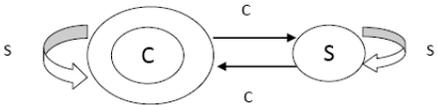
M11



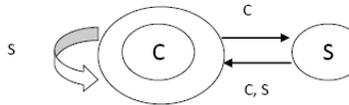
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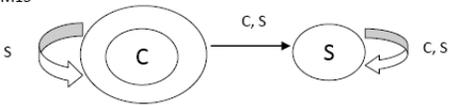
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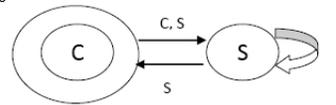
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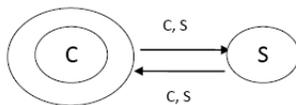
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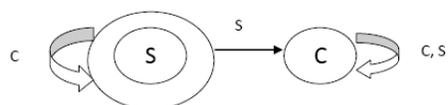
M16



M17



M18



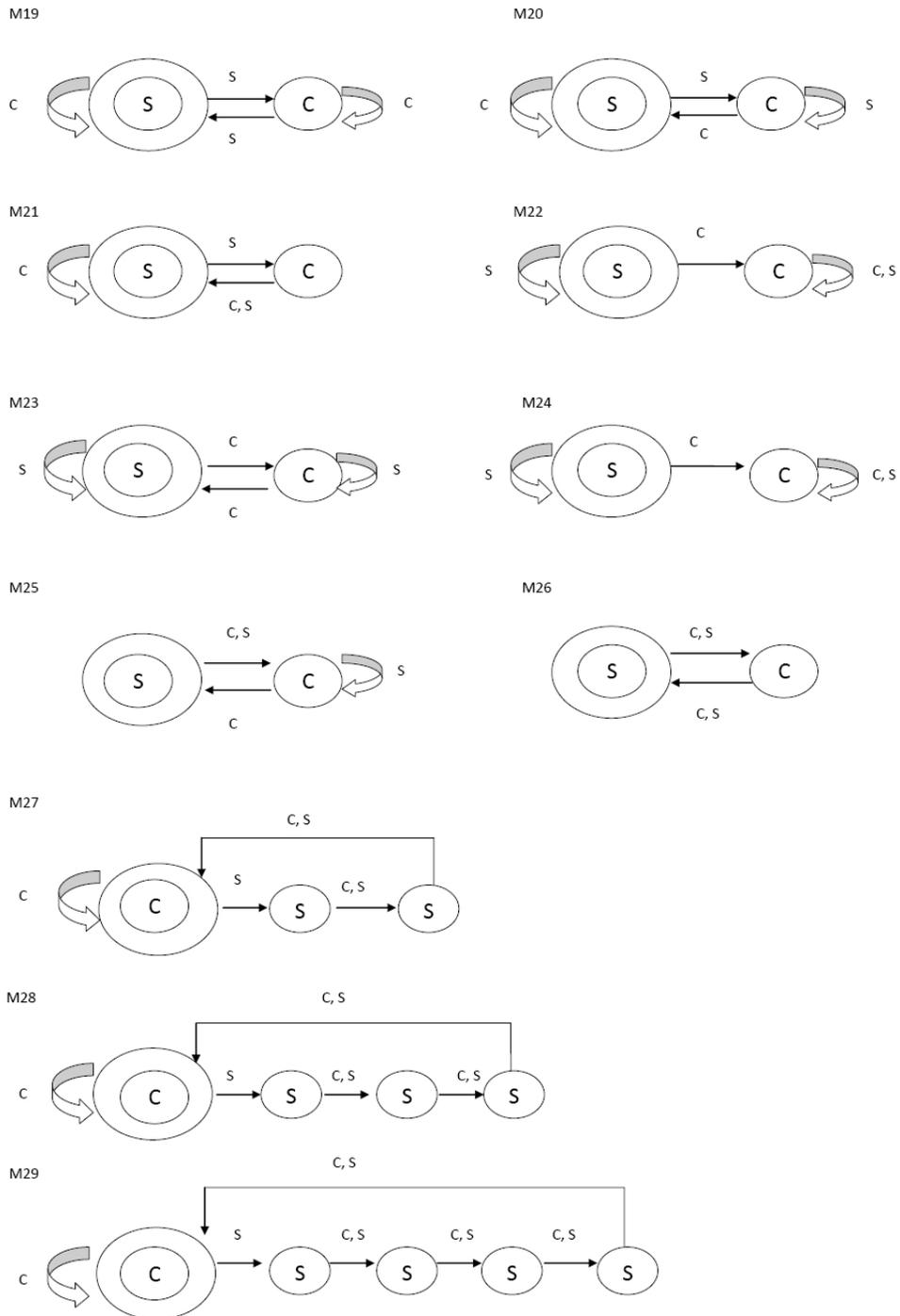


Figure 5: Automata Representation of Repeated Game Strategies

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