

Tossing Game, Grades 5+

What's really going on in the tossing game is something called "modular arithmetic" (more informally known as "clock math"-- can you see why?)

Some online educational articles or websites on modular arithmetic can be found here:

- Blog post that starts from the basics and builds up, including real life applications:
<http://betterexplained.com/articles/fun-with-modular-arithmetic/>
- Slightly more terse article that previous article is based on:
<http://thales.math.uqam.ca/~rowland/investigations/modulararithmetic.html>
- A step-by-step more interactive version by above author:
http://web.math.princeton.edu/math_alive/Crypto/Lab2/ModArithm.html
- Short "simple english" wikipedia article: https://simple.wikipedia.org/wiki/Modular_arithmetic
- An article that starts from the basics and gets pretty advanced!
<https://www.ias.edu/about/publications/ias-letter/articles/2012-summer/modular-arithmetic-taylor>

What is the "passing game"?

- Stephen DeBacker learned this game from Marty Weissman. <http://people.ucsc.edu/~weissman/>
- After defining "modular arithmetic" (or "clock arithmetic" or "circle arithmetic"), n participants stand in a circle with numerical labels, in order from 0 to $n-1$. (The value of n can be changed.)
- The facilitator moderates the game by giving instructions such as:
 - Add 2
 - Add 5
 - Add 3
 - Add 20
 - Multiply by 2
 - Multiply by 10
 - Multiply by 3
 - Square your number
- For each case, you'll observe different patterns and can ask questions for each case such as:
 - Will everyone get the ball? Why or why not? Are some numbers more "fair" than others? Which ones? Why? Does this depend on the total number of people?
 - How long will it take for person j to get the ball back? Is that the same for all people?

Content Areas or Math Practices:

- Division with remainder
- Addition and multiplication
- Factors, Multiples, and Divisibility
- Reasoning, Pattern Recognizing, and Problem-Solving
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